

Soft Spin Physics at Jefferson Lab

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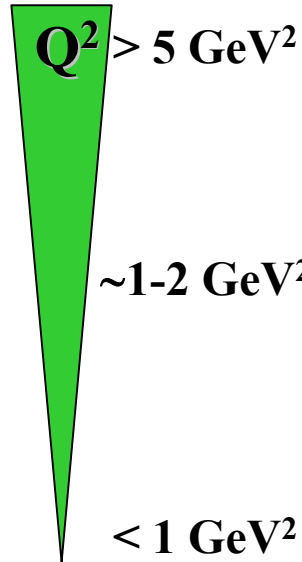
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spin ²⁰⁰⁴ 
16th international spin physics symposium

Outline

- Physics Motivation
- Experimental Setup
- Nucleon Structure Functions at Low Q^2 :
 - ◇ sum rules
 - ◇ resonance contribution and duality
 - ◇ higher twist and soft processes
- Exclusive Measurements and Resonance Contribution
(π^0, π^+, η)

Spin Physics in the non perturbative domain



Measurements of spin observables at large Q^2 allowed the study of the spin dependence of parton distribution functions (CERN, SLAC, DESY)

As Q^2 decreases, non perturbative effects start to play a dominant role and the connection between the nucleon properties and its elementary constituent becomes highly non trivial

At low Q^2 , better description of the nucleon properties can be obtained in terms of hadronic degrees of freedom

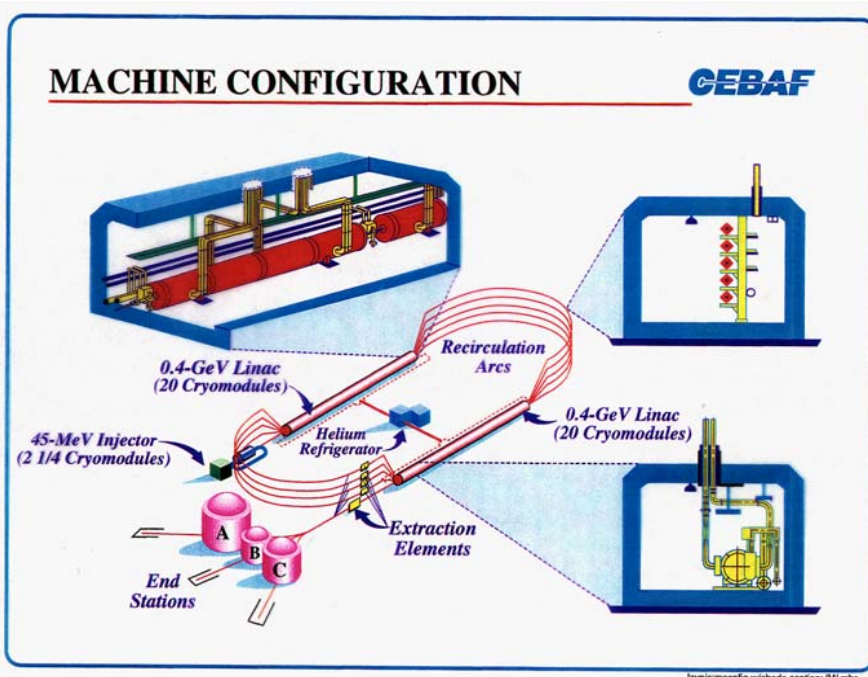
The study of the transition region between hadronic and partonic degrees of freedom is a key issue for the understanding of the nucleon structure

A broad program to study the nucleon spin structure in the soft regime is in progress at Jefferson Lab

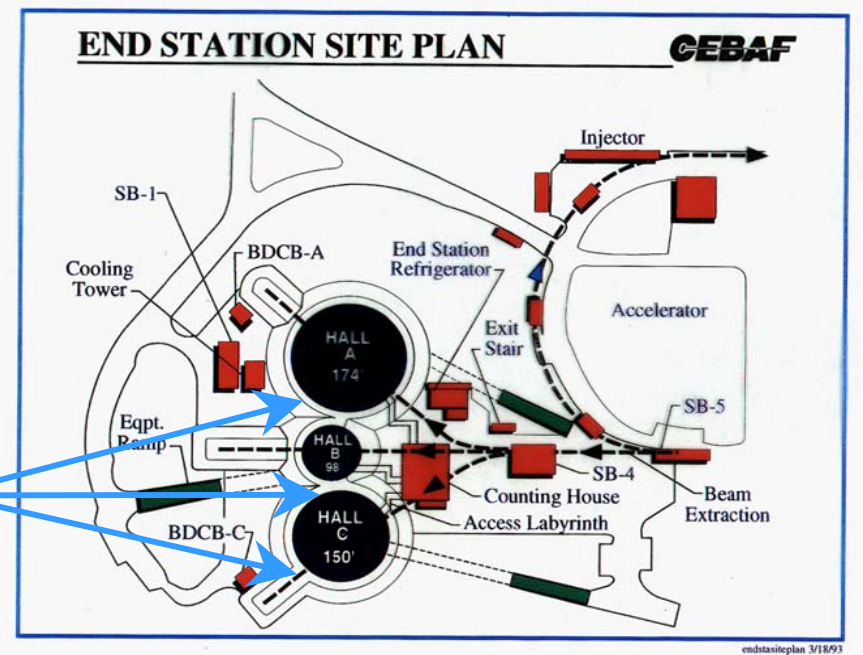
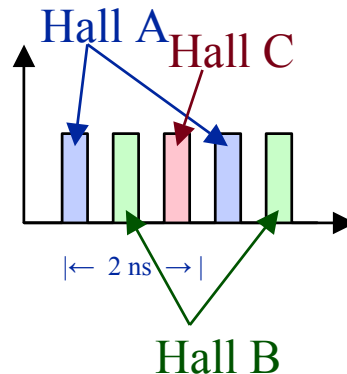
Jefferson Lab

CEBAF is a superconductive electron accelerator

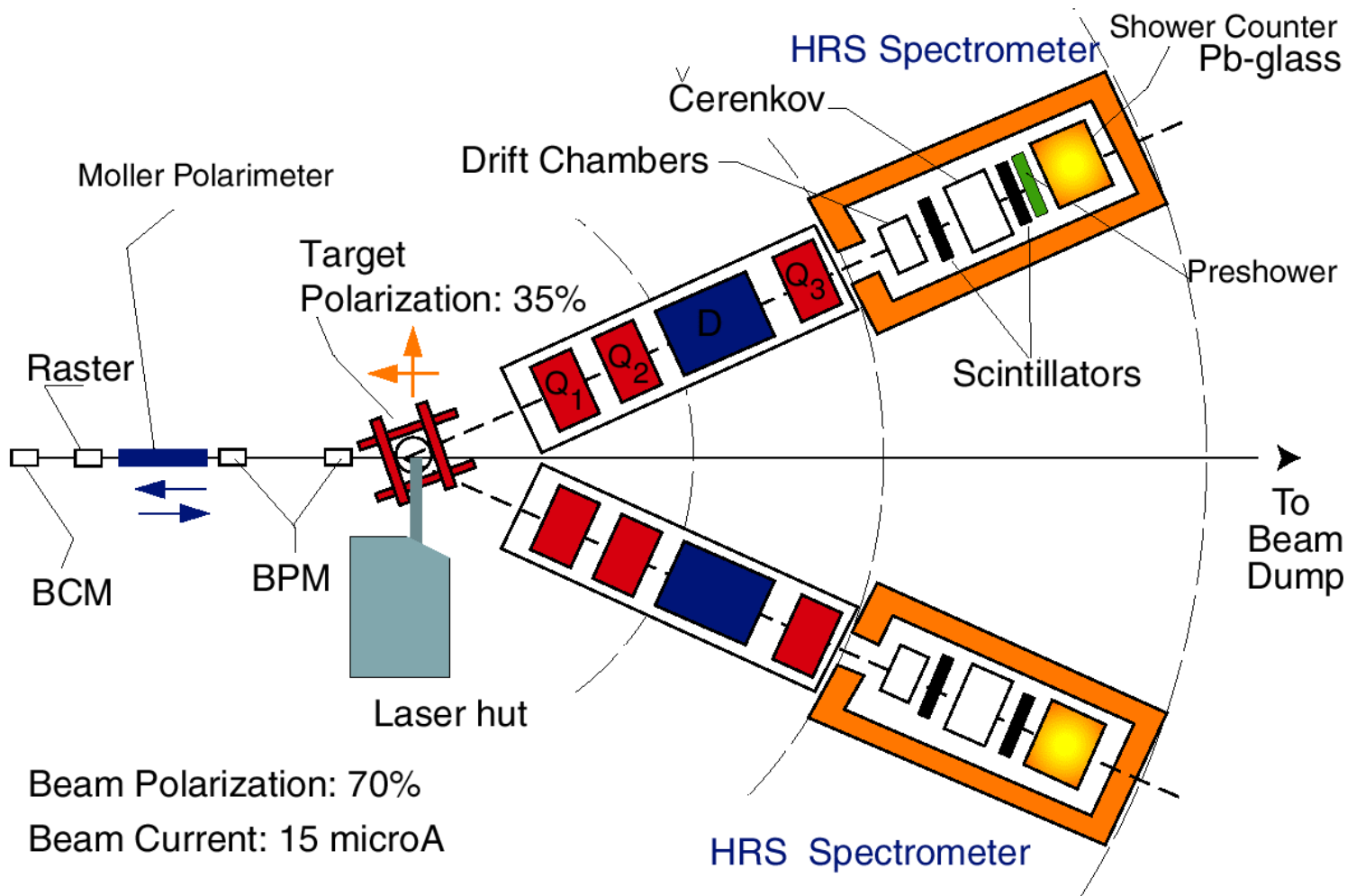
- continuous beam
- high longitudinal polarization
- energy range → 0.75 –5.9 GeV
- current range → 0.1 nA –200mA



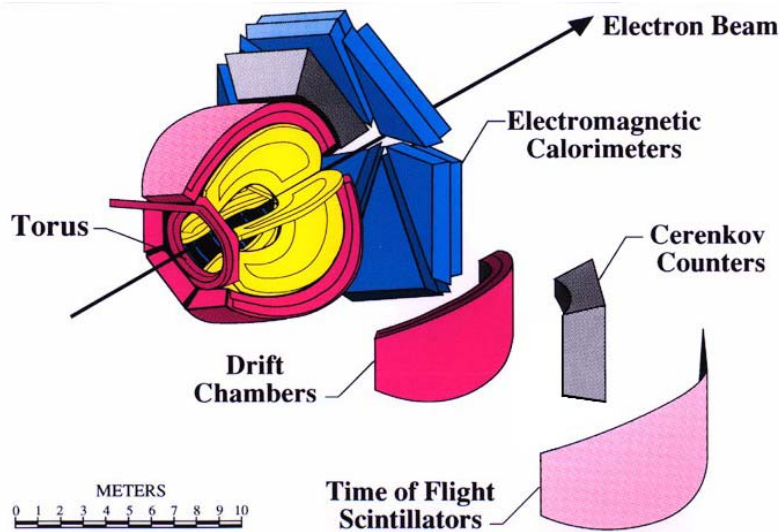
The electron beam can be delivered simultaneously to the three halls with high polarization



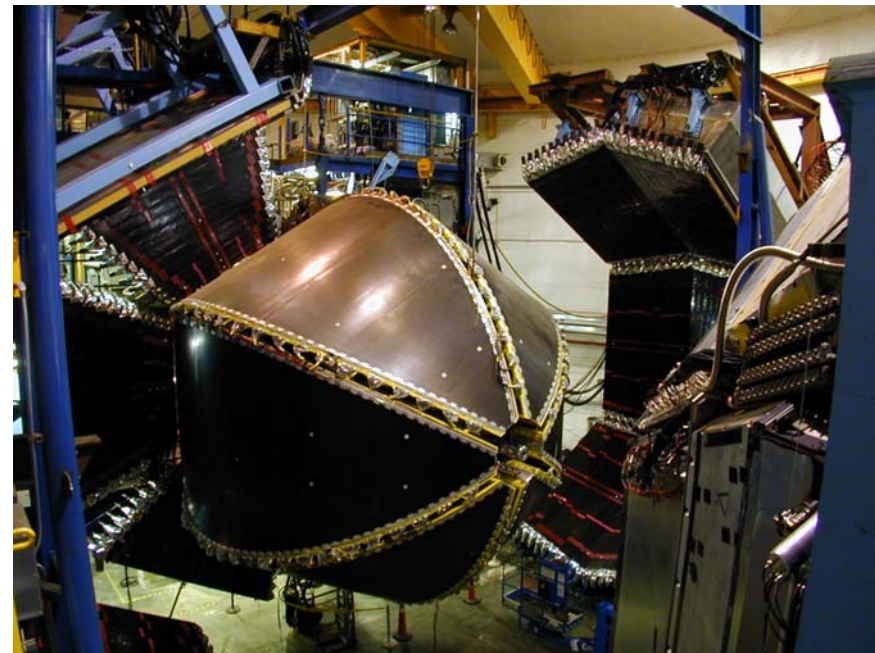
Experimental Setup: Hall A



Experimental Setup: Hall B

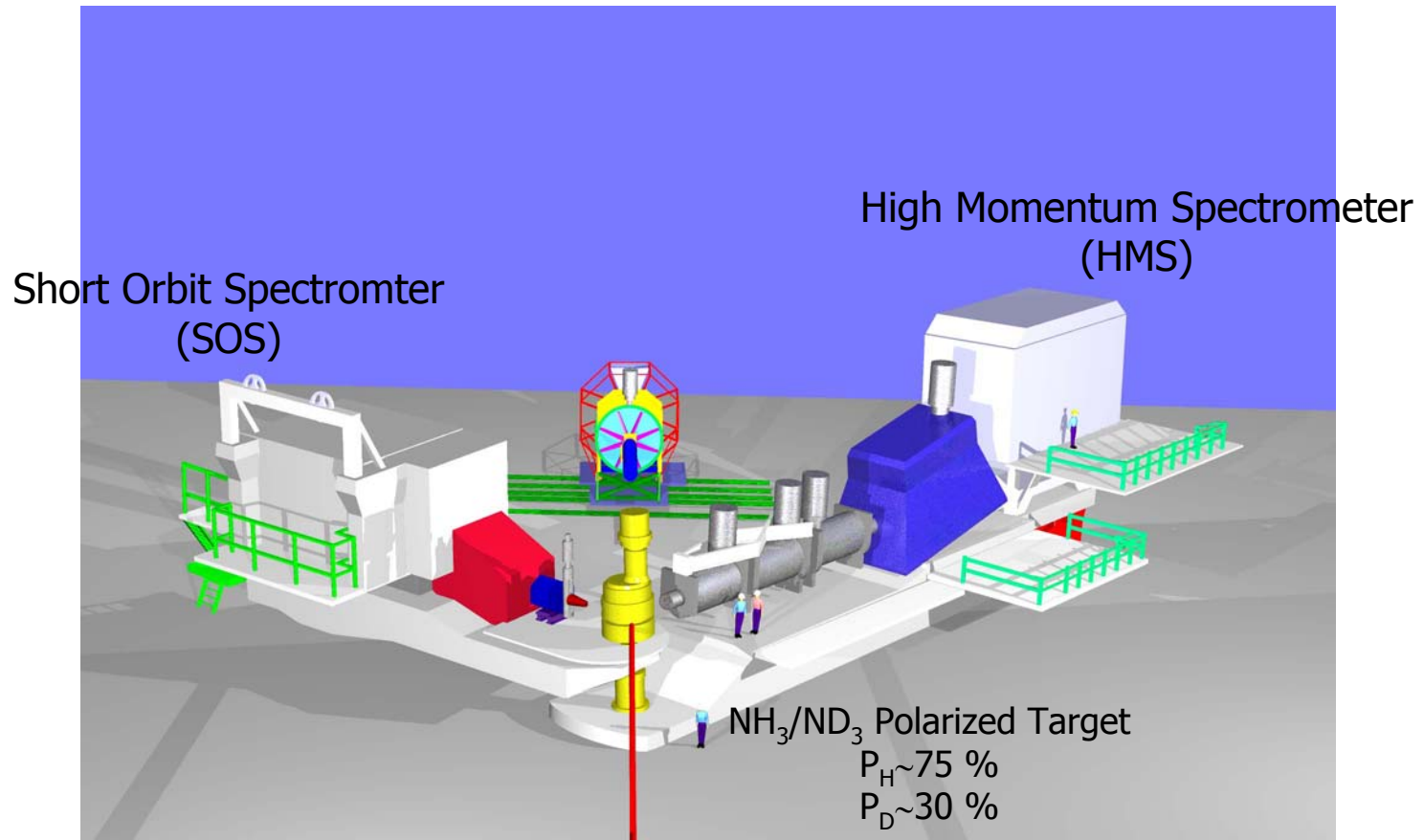


CEBAF
Large
Acceptance
Spectrometer



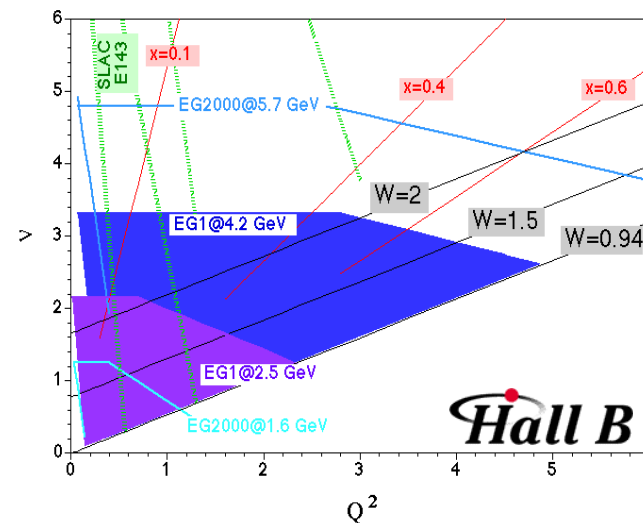
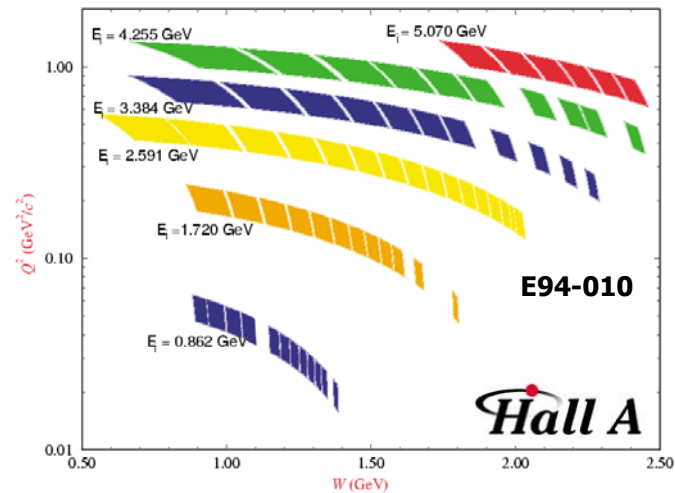
- ◆ large kinematical coverage
- ◆ simultaneous measurement of exclusive and inclusive reactions
- ◆ central field-free region well suited for the insertion of the polarized target

Experimental Setup: Hall C



Experimental Program

- ◆ measurement of the nucleon spin structure functions in the resonance region
- ◆ test of the generalized Gerasimov-Drell-Hearn Sum Rule on the proton and neutron
- ◆ measurement of nucleon spin polarizabilities at low Q^2
- ◆ test of duality of spin structure function
- ◆ extraction of the moments of the proton and neutron structure functions and study of higher twist contribution
- ◆ study of the nucleon resonance structure from polarization observables in exclusive meson production



Sum Rules and Integrals of Spin Structure Functions

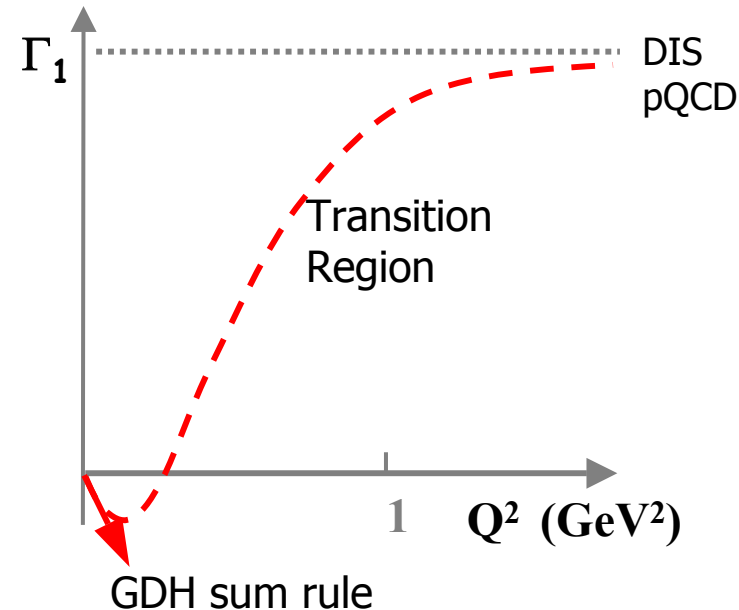
GDH Sum Rule

$$I_{GDH} = \frac{M^2}{8\alpha\pi^2} \int_{thr}^{\infty} (\sigma_{1/2} - \sigma_{3/2}) \frac{d\nu}{\nu} = -\frac{1}{4} \kappa^2$$

- ◆ relates the difference of the photo-absorption cross section for helicity 1/2 and 3/2 to the nucleon magnetic moment, i.e. a connection between dynamic and static properties
- ◆ based on very general principles, as gauge invariance, dispersion relation, low energy theorem
- ◆ at finite Q^2 can be related to the integral of the spin structure function g_1

$$\Gamma_1 = \int g_1(x, Q^2) dx \xrightarrow{Q^2 \rightarrow 0} \frac{Q^2}{2M^2} I_{GDH}$$

- ◆ strong variation of nucleon spin properties as a function of Q^2



Generalized GDH Integral

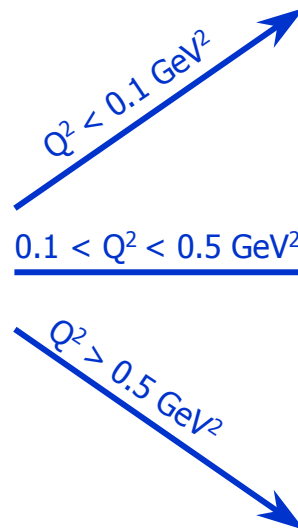
A generalization of the GDH sum rule has been suggested by Ji and Osborne by relating the virtual-photon forward Compton amplitude to the nucleon structure function Γ_1

X.Ji et al., Phys.Lett.B472 (2000) 1

$$I_{\text{GDH}}(Q^2) = \frac{8}{Q^2} \int_{x_0}^{\infty} dx g_1(x, Q^2)$$

the left side is a calculable quantity

the right side is a measurable quantity



GDH sum rule and Chiral Perturbation Theory

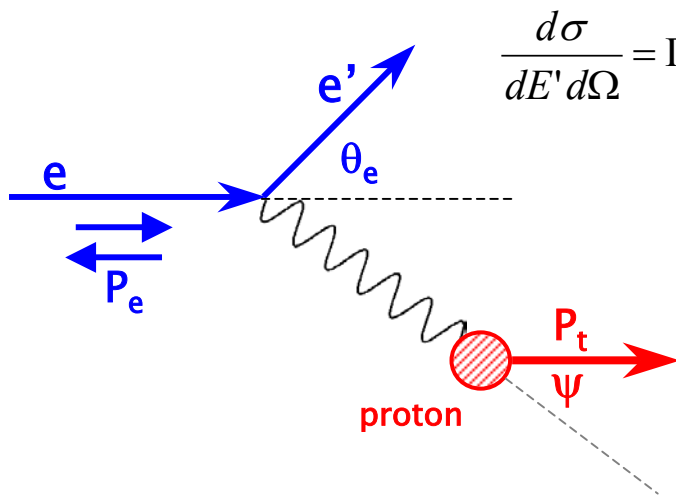
$$-\frac{\kappa^2}{M^2} + cQ^2 + O(Q^4)$$

Lattice?

Bjorken Sum rule and Operator Product Expansion

$$\sim \sum_{\tau=2,4,\dots} \frac{\mu_{\tau}(Q^2)}{Q^{\tau-2}}$$

Asymmetries and Spin Structure Functions



$$\frac{d\sigma}{dE' d\Omega} = \Gamma_v \left[\sigma_T + \varepsilon \sigma_L + P_e P_t \left(\sqrt{1 - \varepsilon^2} \mathbf{A}_1 \sigma_T \cos \psi + \sqrt{2\varepsilon(1 - \varepsilon)} \mathbf{A}_2 \sigma_T \sin \psi \right) \right]$$

$$\mathbf{A}_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_T} \quad \mathbf{A}_2 = \frac{\sigma_{LT'}}{\sigma_T}$$

the structure functions \mathbf{A}_1 and \mathbf{A}_2 can be extracted by varying the direction of the nucleon polarization

$$A^{\parallel} = D(A_1 + \eta A_2)$$

$$A^{\perp} = d(A_1 + \zeta A_2)$$

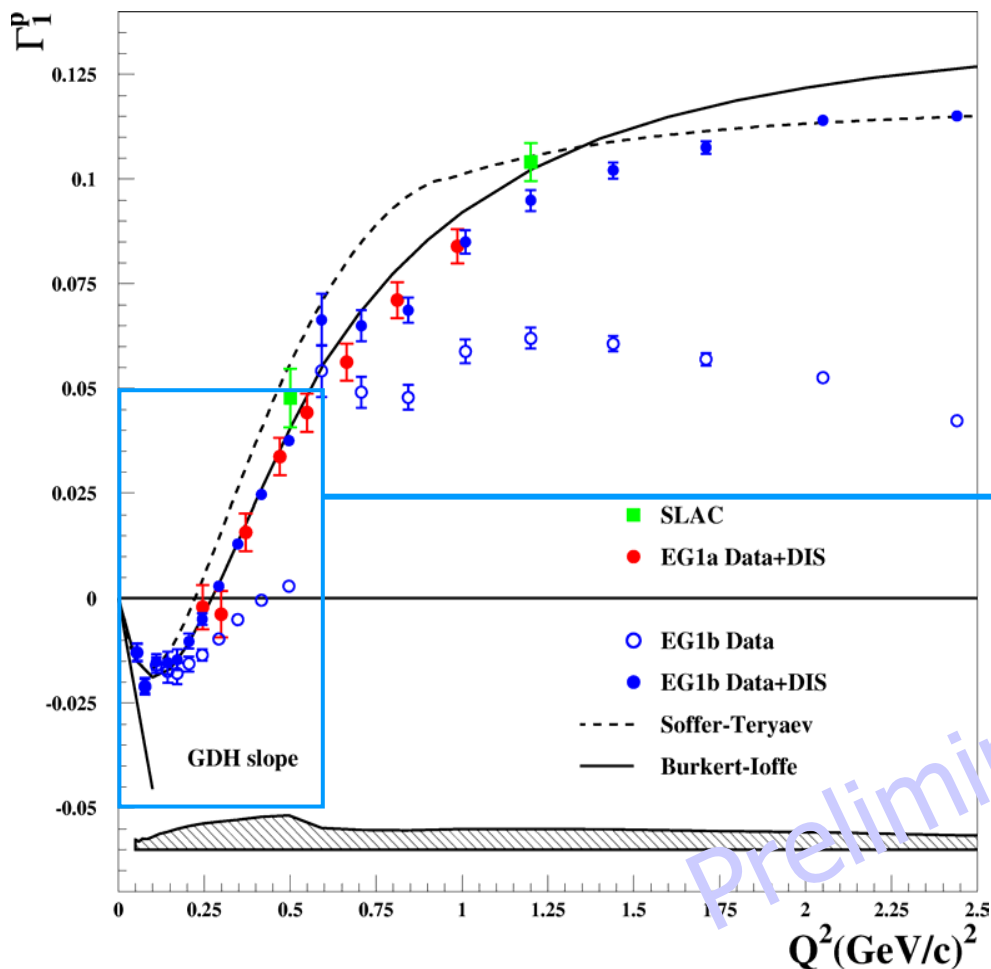
where D , η , d , ζ are function of Q^2 , W , E_0 , R

the structure functions \mathbf{g}_1 and \mathbf{g}_2 are linear combination of \mathbf{A}_1 and \mathbf{A}_2

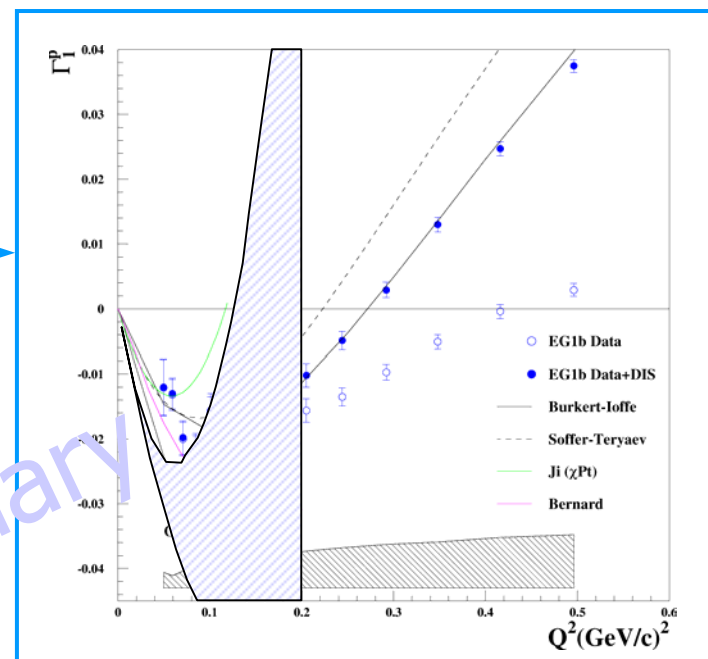
$$\mathbf{g}_1(\mathbf{x}, Q^2) = \frac{Q^2}{Q^2 + 4M^2 x^2} \left(A_1 + \frac{2Mx}{\sqrt{Q^2}} A_2 \right) F_1(x, Q^2)$$

$$\mathbf{g}_2(\mathbf{x}, Q^2) = \frac{Q^2}{Q^2 + 4M^2 x^2} \left(\frac{\sqrt{Q^2}}{2Mx} A_2 - A_1 \right) F_1(x, Q^2)$$

Integral of g_1 on the Proton

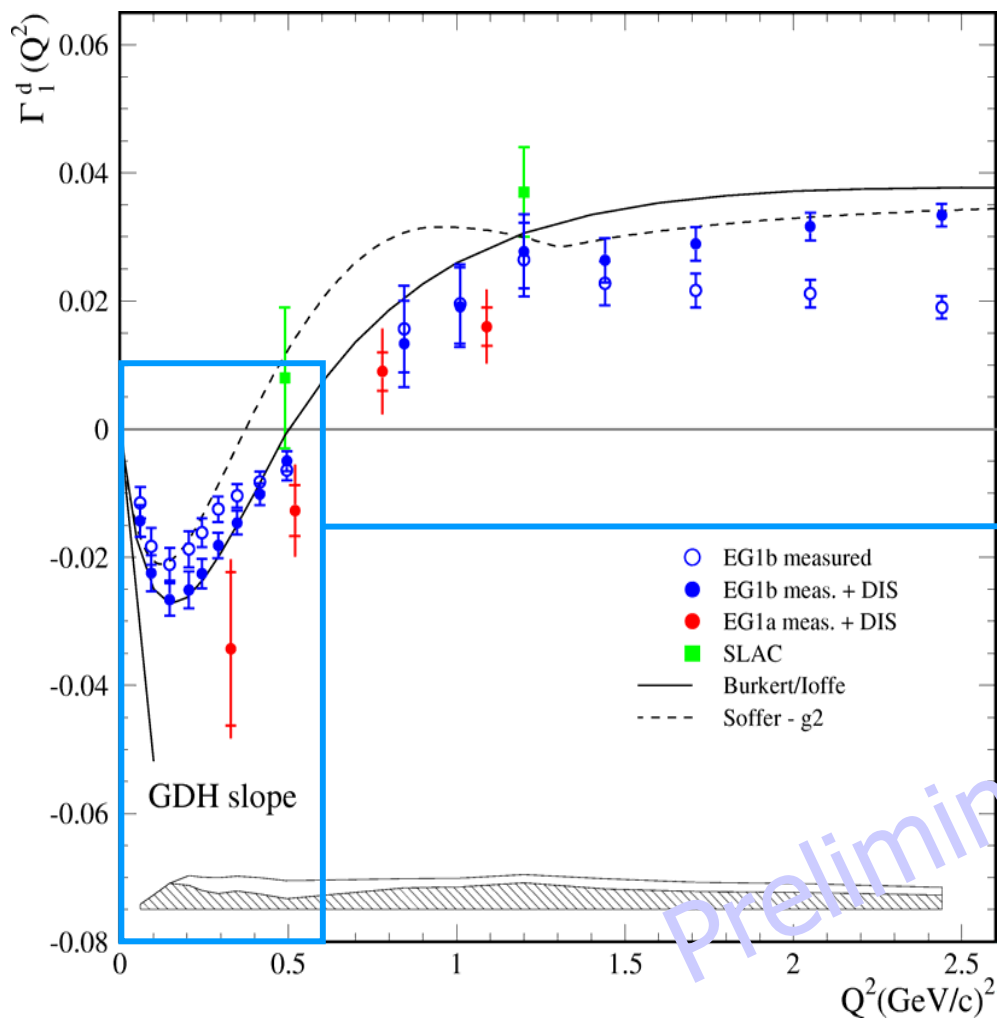


- ◆ consistent with previous SLAC data
- ◆ shows strong Q^2 dependence
- ◆ change in slope occurs at 0.15 GeV^2

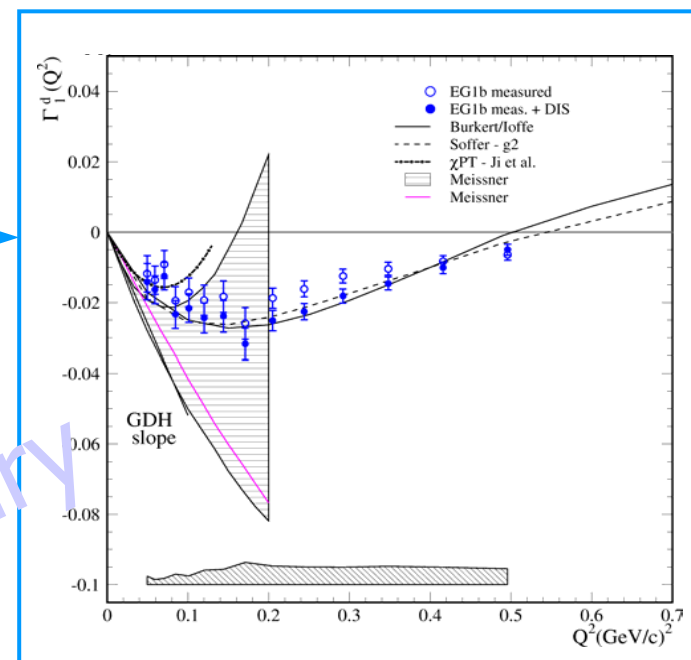


Preliminary

Integral of g_1 on the Deuteron

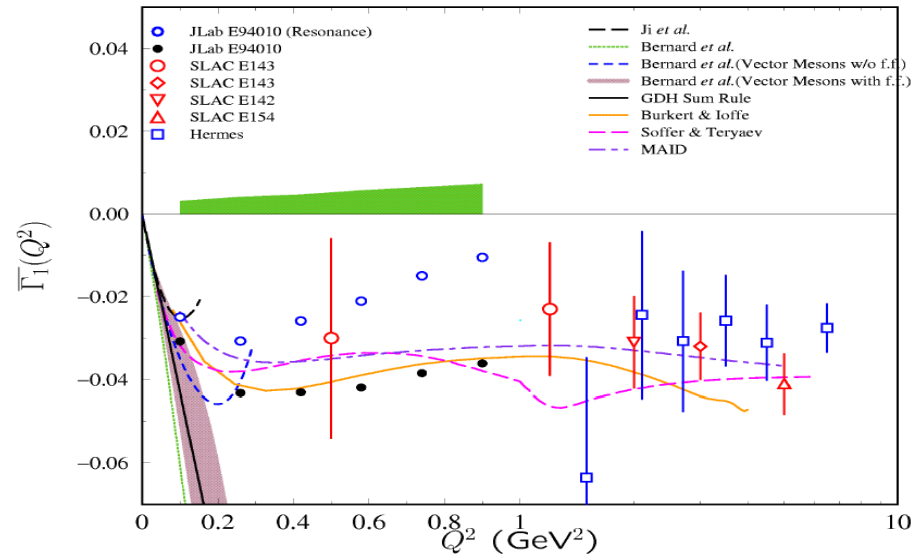


- ◆ consistent with previous SLAC data
- ◆ slower transition than for the proton
- ◆ change in slope occurs at 0.2 GeV^2



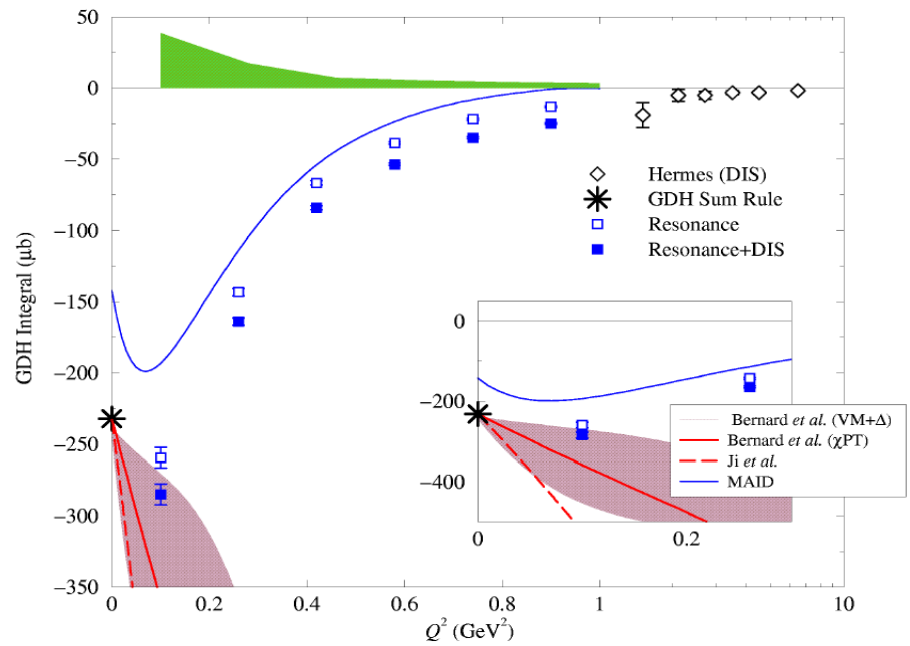
Preliminary

g_1 and GDH Integral on the Neutron



- ◆ strong variation of GDH integral from 0.1 to 1. GeV^2
- ◆ integral starts to approach Sum Rule at $Q^2=0.1 \text{ GeV}^2$
- ◆ first point consistent with χPT prediction

- ◆ complementary to Hall B because of different target and analysis procedure
- ◆ consistent with previous SLAC data
- ◆ integral is negative and shows smooth Q^2 dependence

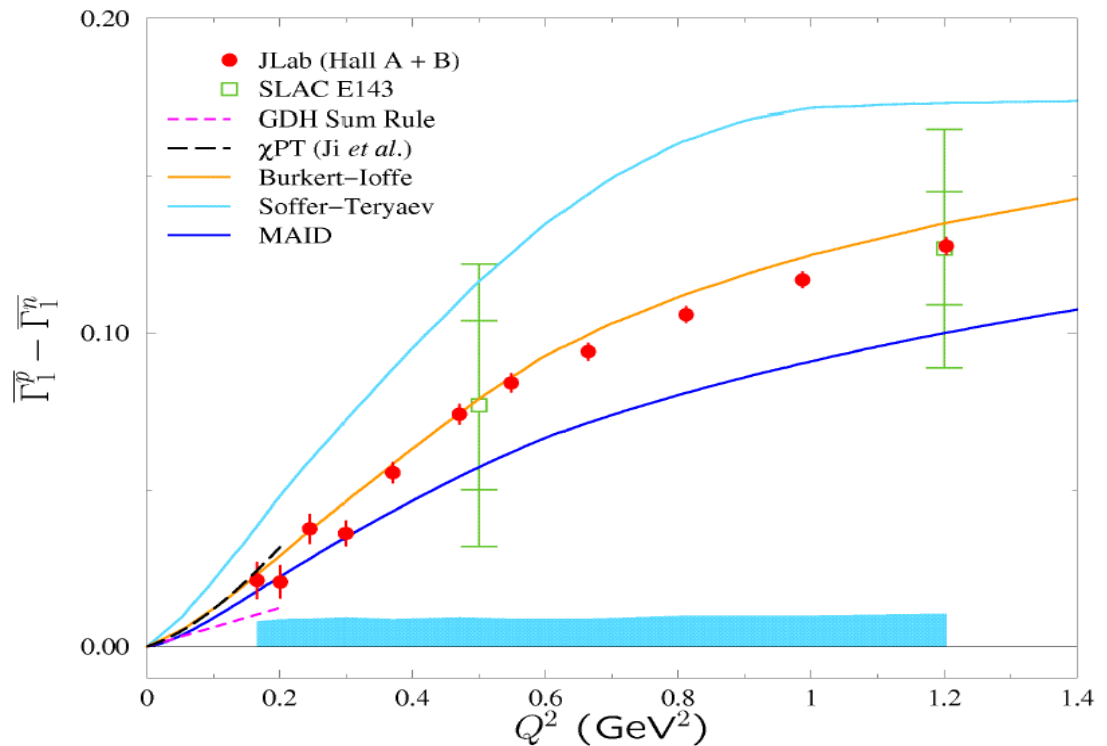


Bjorken Sum Rule

$$\Gamma_1^p - \Gamma_1^n = \int (g_1^p - g_1^n) dx \xrightarrow{Q^2 \rightarrow \infty} \frac{g_a}{6}$$

→ see talk by A. Deur

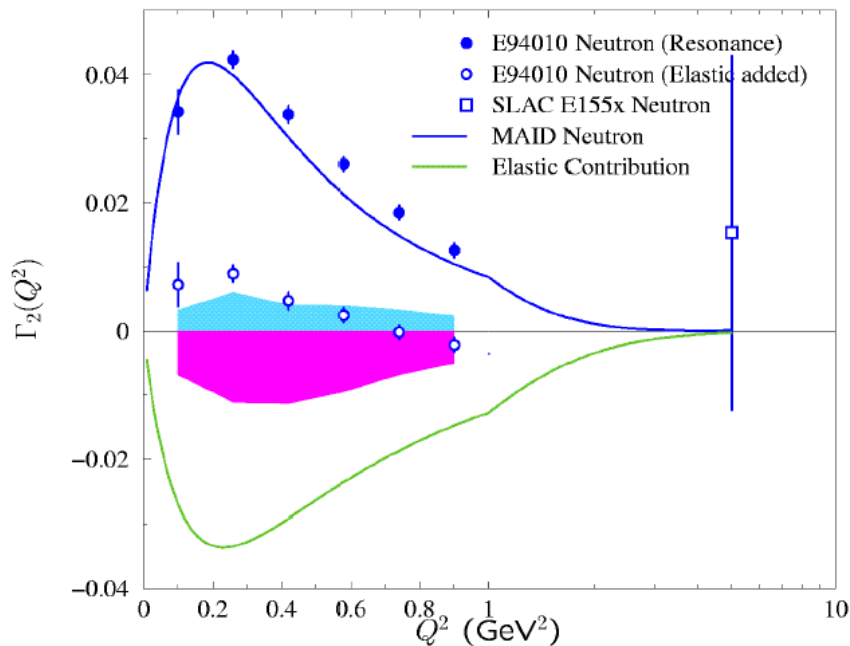
- ◆ combined analysis of Hall A and Hall B measurements
- ◆ consistent with previous SLAC data
- ◆ Δ and other isospin 3/2 contribution cancel out
- ◆ better agreement with χ PT than for separated proton and neutron integrals



Integral of g_2 on the Neutron

(Burkardt-Cottingham Sum Rule)

$$\Gamma_2(Q^2) \equiv \int_0^1 g_2(x, Q^2) dx = 0$$



- From superconvergence of corresponding Compton Amplitude
- Valid for *every* Q^2
- No confirmation from Operator Product Expansion
- At $Q^2 = 5 \text{ GeV}^2$, possible satisfaction from SLAC E155x

Spin Polarizabilities

Virtual Compton Scattering

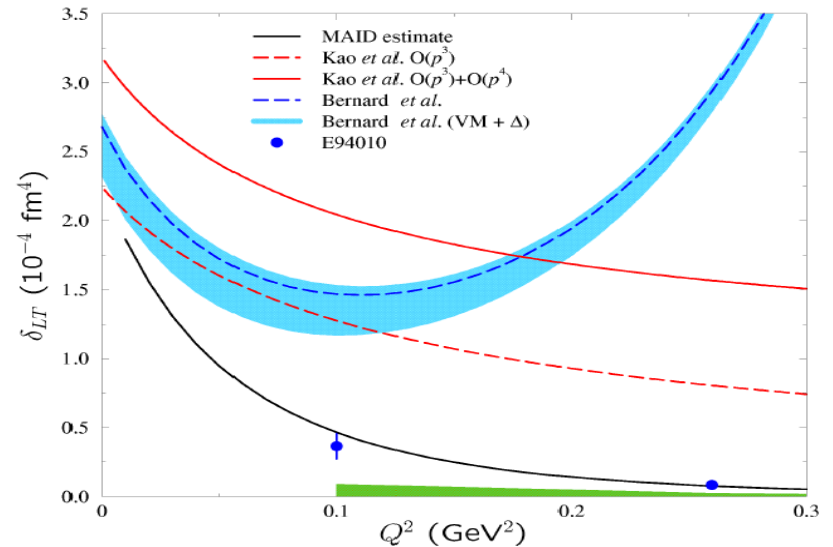
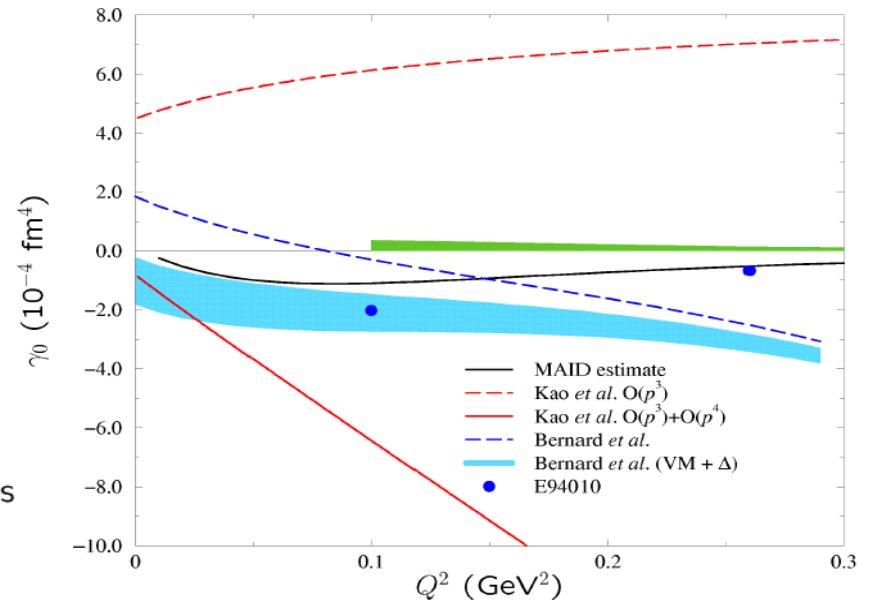
$$T(\nu, Q^2) = \varepsilon'^* \cdot \varepsilon f_T(\nu, Q^2) + f_L(\nu, Q^2) + i\sigma \cdot (\varepsilon'^* \times \varepsilon) g_{TT}(\nu, Q^2) - i\sigma \cdot [(\varepsilon'^* - \varepsilon) \times \hat{q}] g_{LT}(\nu, Q^2)$$

- $f_T \rightarrow \alpha + \beta$ electric and magnetic polarizabilities
- $g_{TT} \rightarrow \gamma_0$ forward spin polarizability
- $f_L \rightarrow \alpha_L$ longitudinal polarizability
- $g_{LT} \rightarrow \delta_{LT}$ longitudinal-transverse polarizability

$$\gamma_0(Q^2) = \frac{16M^2\alpha_{em}}{Q^6} \int_0^{x_0} x^2 \left\{ g_1(x, Q^2) - \frac{Q^2}{\nu^2} g_2(x, Q^2) \right\} dx$$

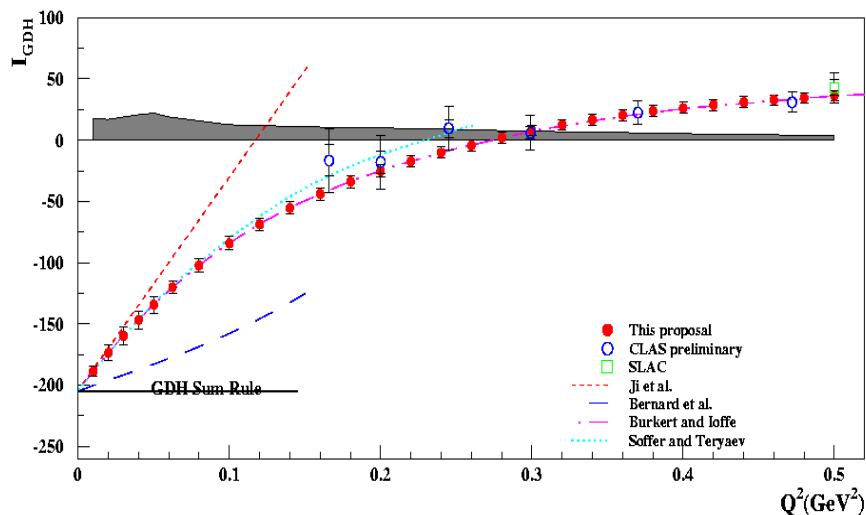
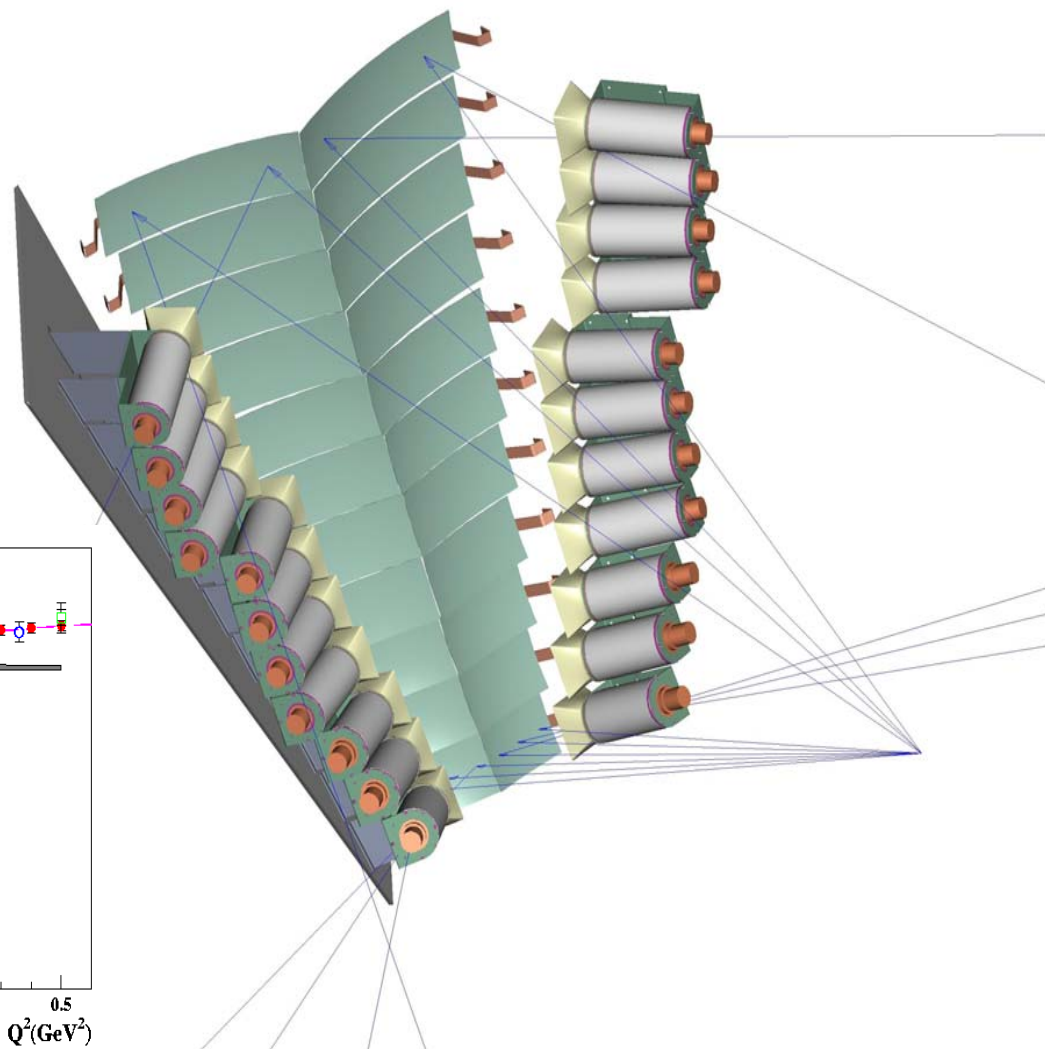
$$\delta_{LT}(Q^2) = \frac{16M^2\alpha_{em}}{Q^6} \int_0^{x_0} x^2 \left\{ g_1(x, Q^2) + g_2(x, Q^2) \right\} dx$$

$$\delta_{LT}(Q^2) \rightarrow \frac{1}{3}\gamma_0(Q^2), \quad Q^2 \rightarrow \infty$$



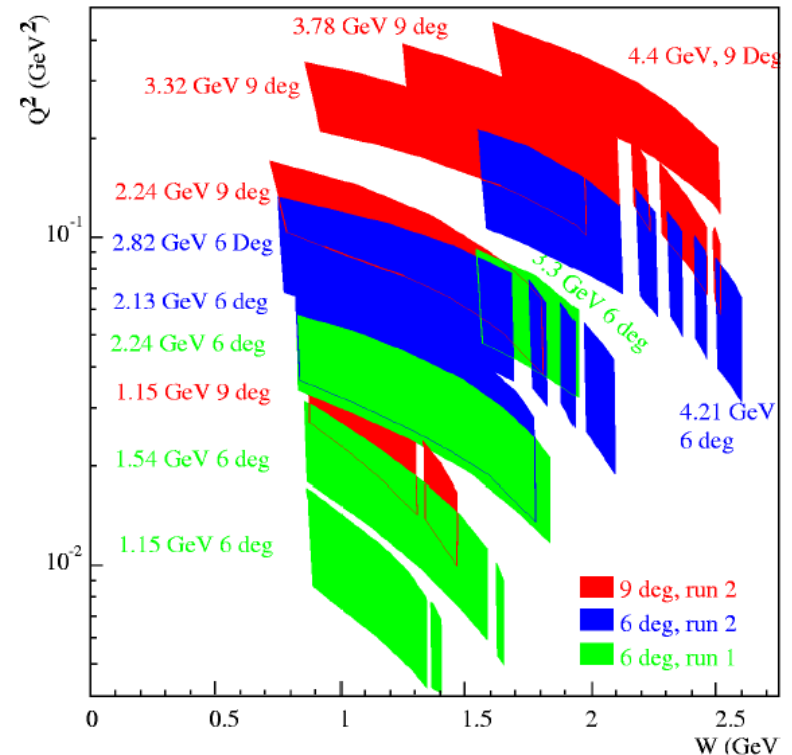
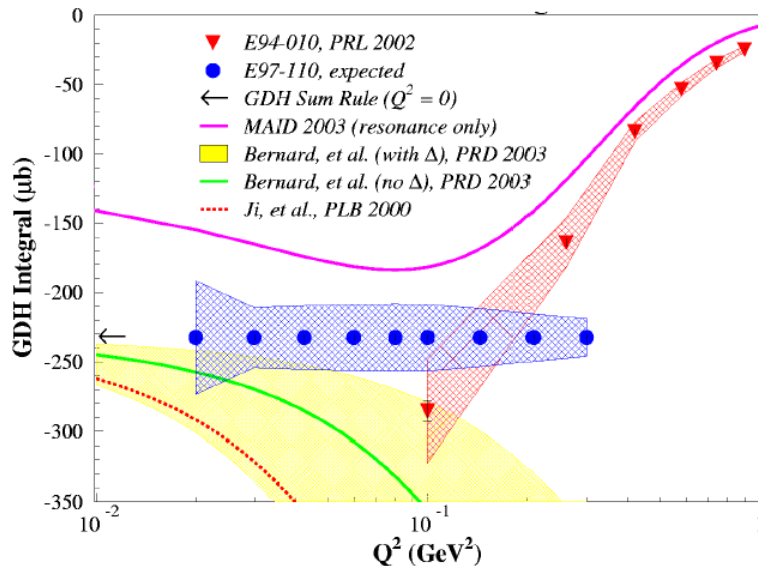
Proton Structure Function at Very Low Q^2

- ◆ Extension of previous experiments
- ◆ Test of χ PT at $Q^2 \rightarrow 0$
- ◆ New Cerenkov Counter to detect scattered electrons at 5 deg. (INFN-Genova)



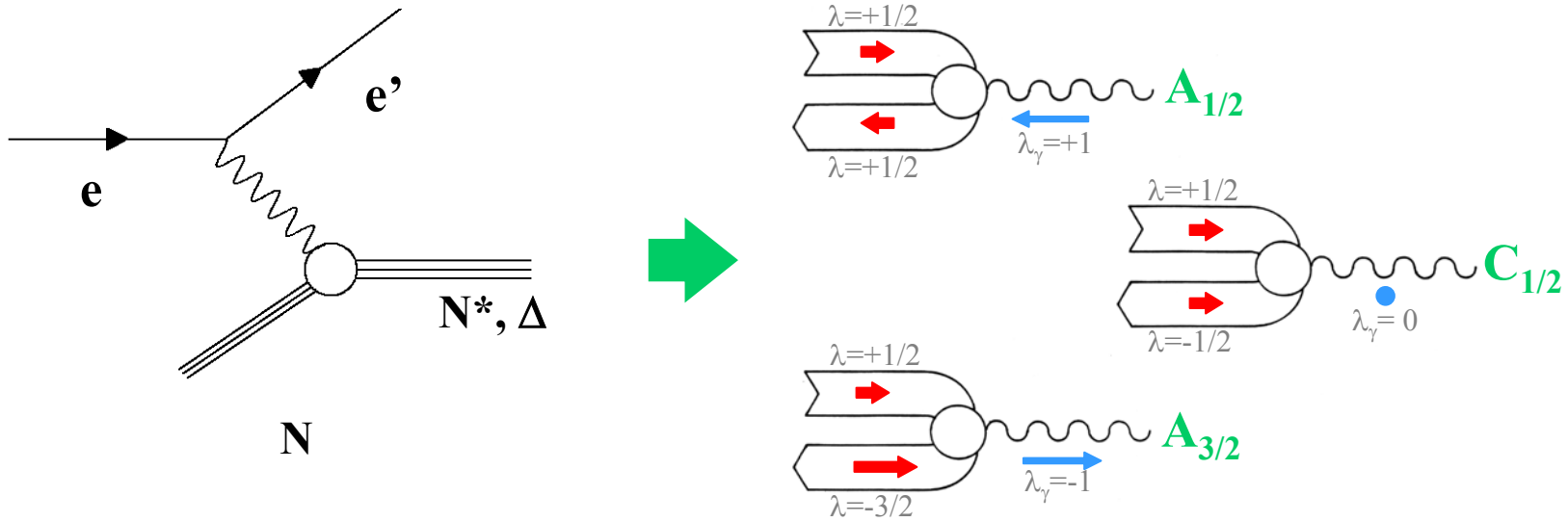
Neutron Structure Function at Very Low Q^2

- ◆ Extension of previous experiments
- ◆ Test of χ PT at $Q^2 \rightarrow 0$
- ◆ Data taking completed in 2003, analysis in progress



Resonance Contribution to Spin Structure Functions and Duality

Helicity Structure of Baryon Resonances



- the helicity amplitudes provide information on the structure of the excited states
- their Q^2 dependence is determined by the spatial structure of the excited state
- polarization measurements are necessary to extract the helicity amplitudes

$$\sigma_T = \sigma_{1/2} + \sigma_{3/2} = |A_{1/2}|^2 + |A_{3/2}|^2$$

$$A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_T} \rightarrow |A_{1/2}|^2 - |A_{3/2}|^2$$

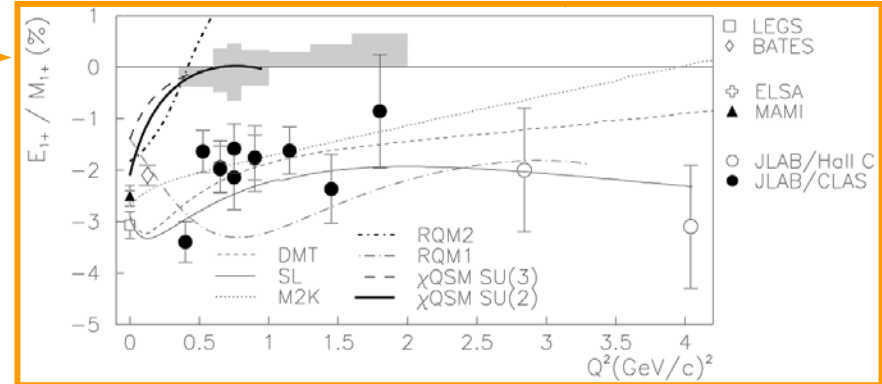
$$A_2 = \frac{\sigma_{LT}}{\sigma_T} \rightarrow C_{1/2}^* A_{1/2}$$

Helicity Structure of Baryon Resonances

$P_{33}(1232)$

the helicity asymmetry can be written in the assumption of M_{1+} dominance as

$$A_1 \approx -\frac{1}{2} + 3 \frac{\text{Re}(E_{1+}^* M_{1+})}{|M_{1+}|^2}$$



$P_{11}(1440) - S_{11}(1535)$

$$A_1 = 1$$

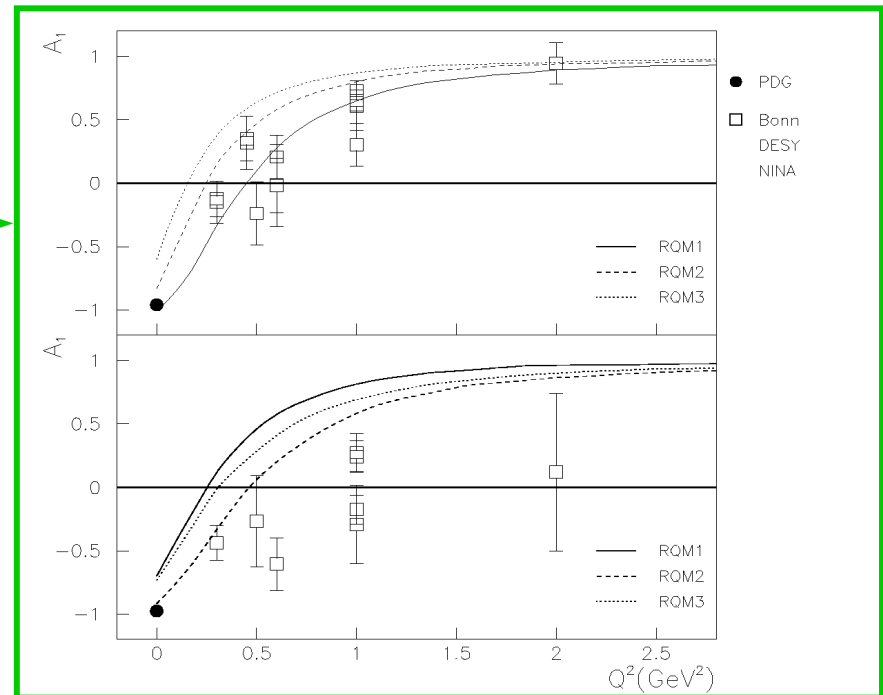
$D_{13}(1520) - F_{15}(1680)$

the helicity asymmetry is predicted by the NRQM to be

$$A_1 = \frac{-1 + [(\vec{q}^2/\alpha^2 - 1)/3]^2}{1 + [(\vec{q}^2/\alpha^2 - 1)/3]^2}$$

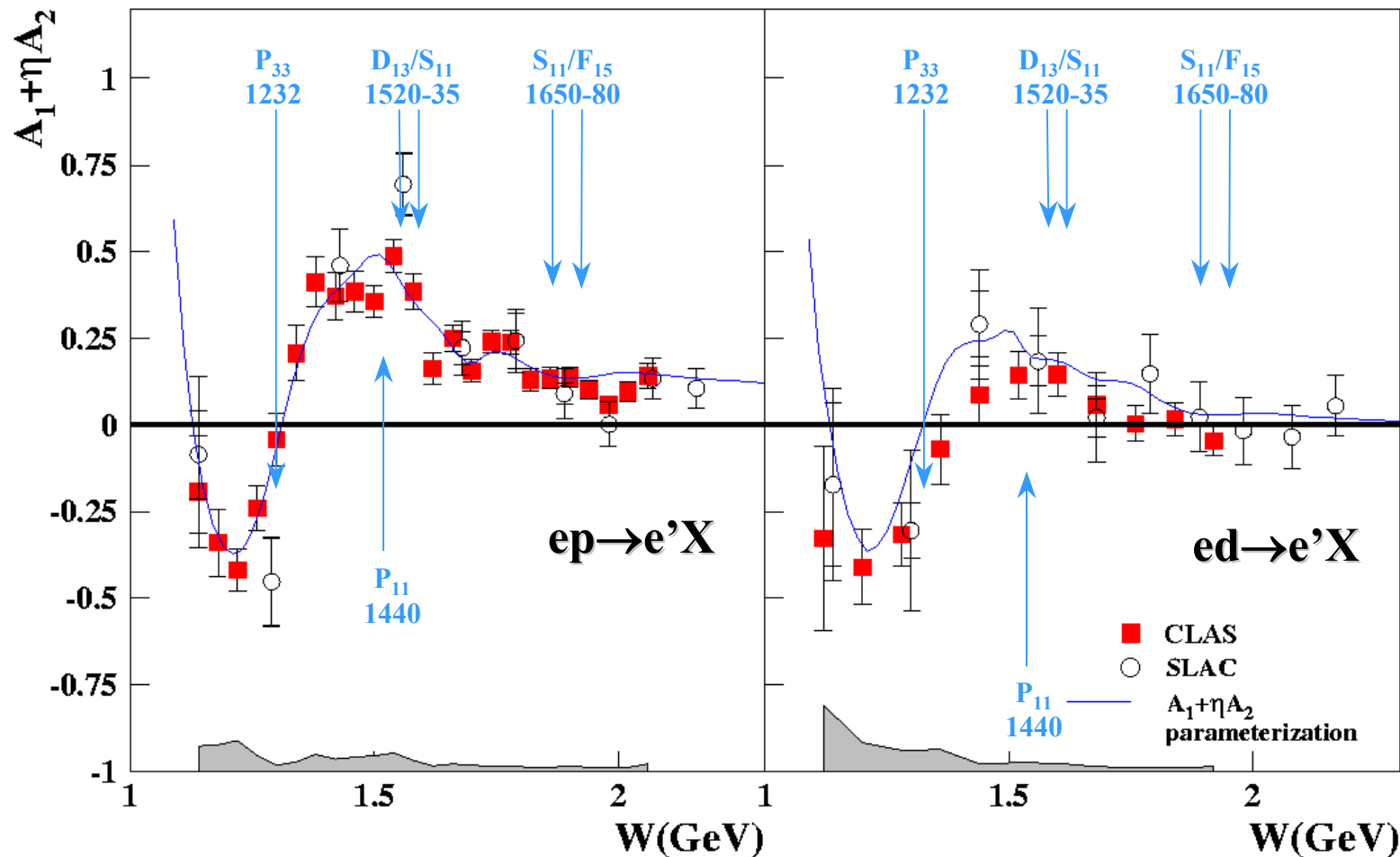
$$\xrightarrow{Q^2 \rightarrow 0} -1$$

$$\xrightarrow{Q^2 \rightarrow \infty} +1$$



$A_1 + \eta A_2$ for proton and deuteron

$0.4 < Q^2 < 0.6 \text{ GeV}^2$



$A_{||}$ and A_{\perp} for proton and deuteron

E01-006

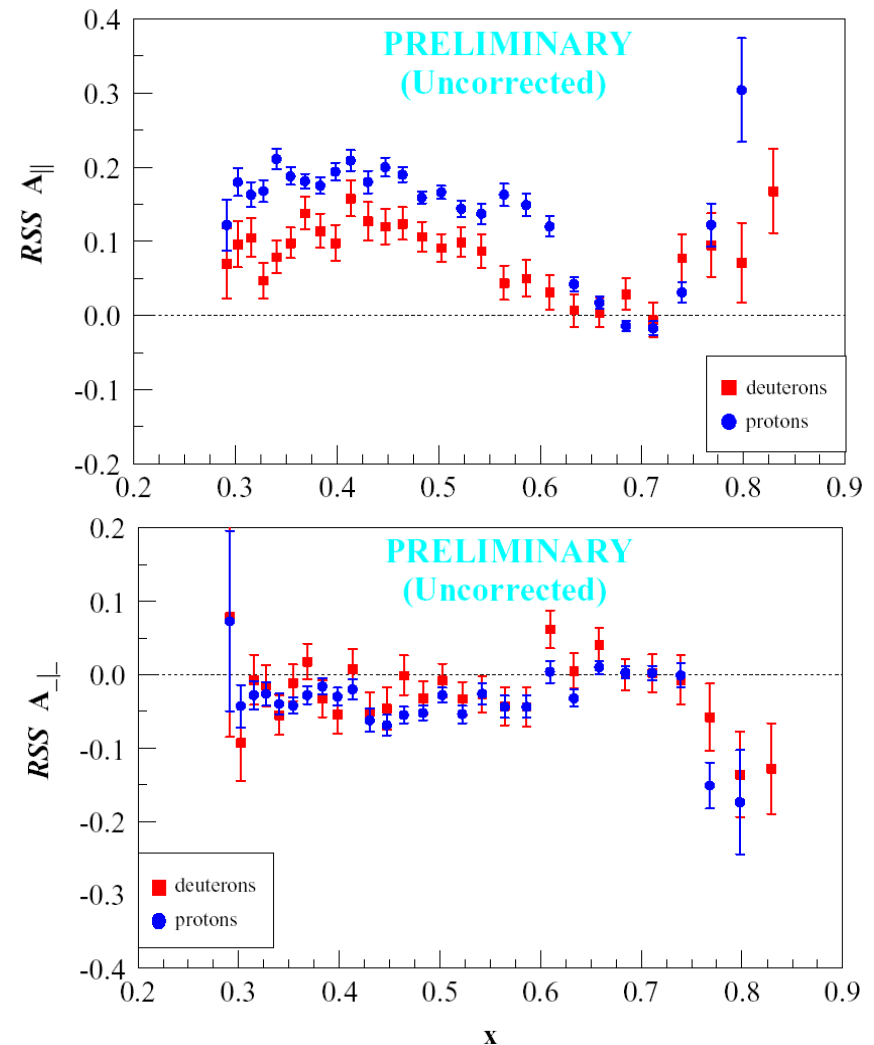
Precision of the Nucleon Spin Structure Functions in the Resonance Region

$$\theta_e = 13.5^\circ$$

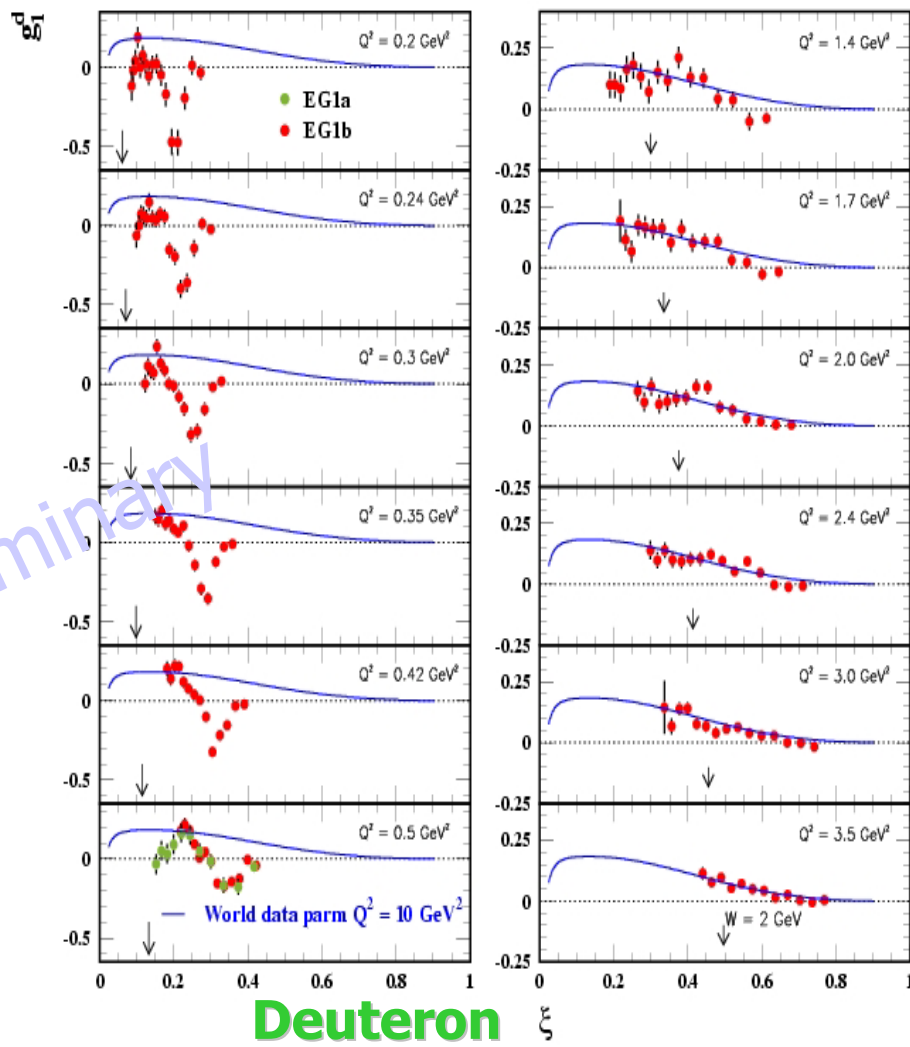
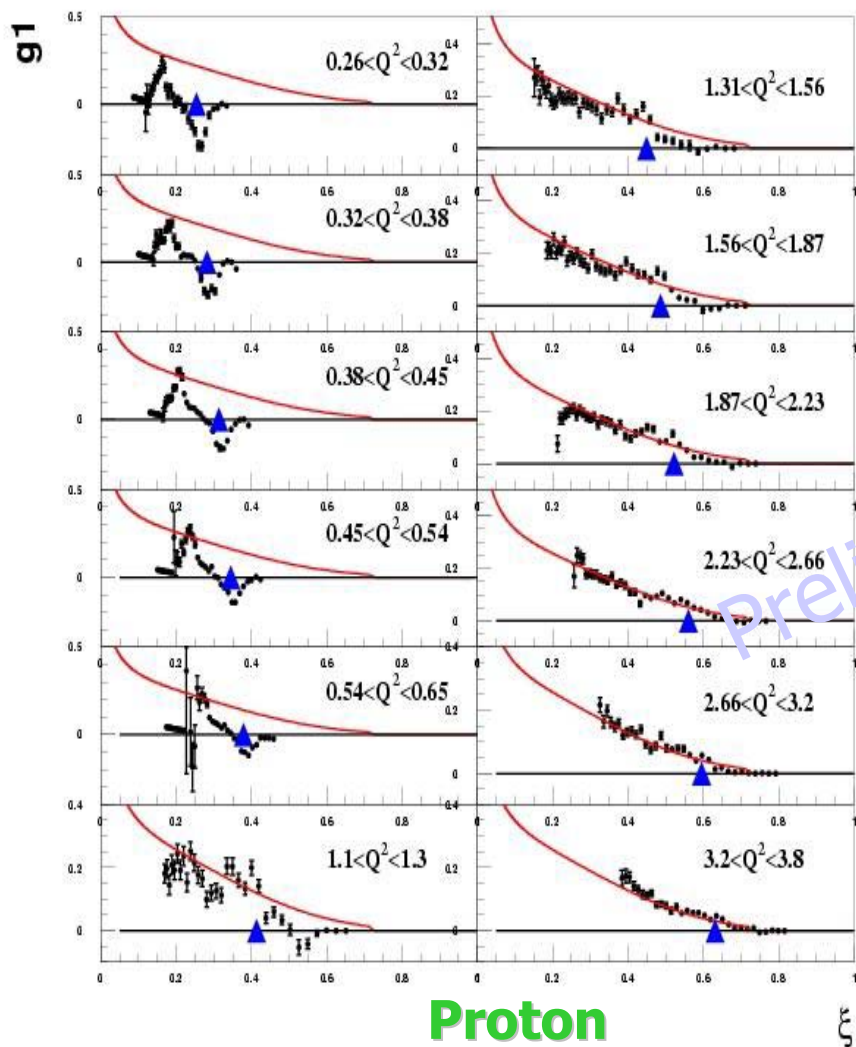
$$Q^2 \approx 1.3 \text{ GeV}^2$$

$$0.8 < W < 2.0 \text{ GeV}$$

Analysis in progress



Duality in Spin Structure Functions



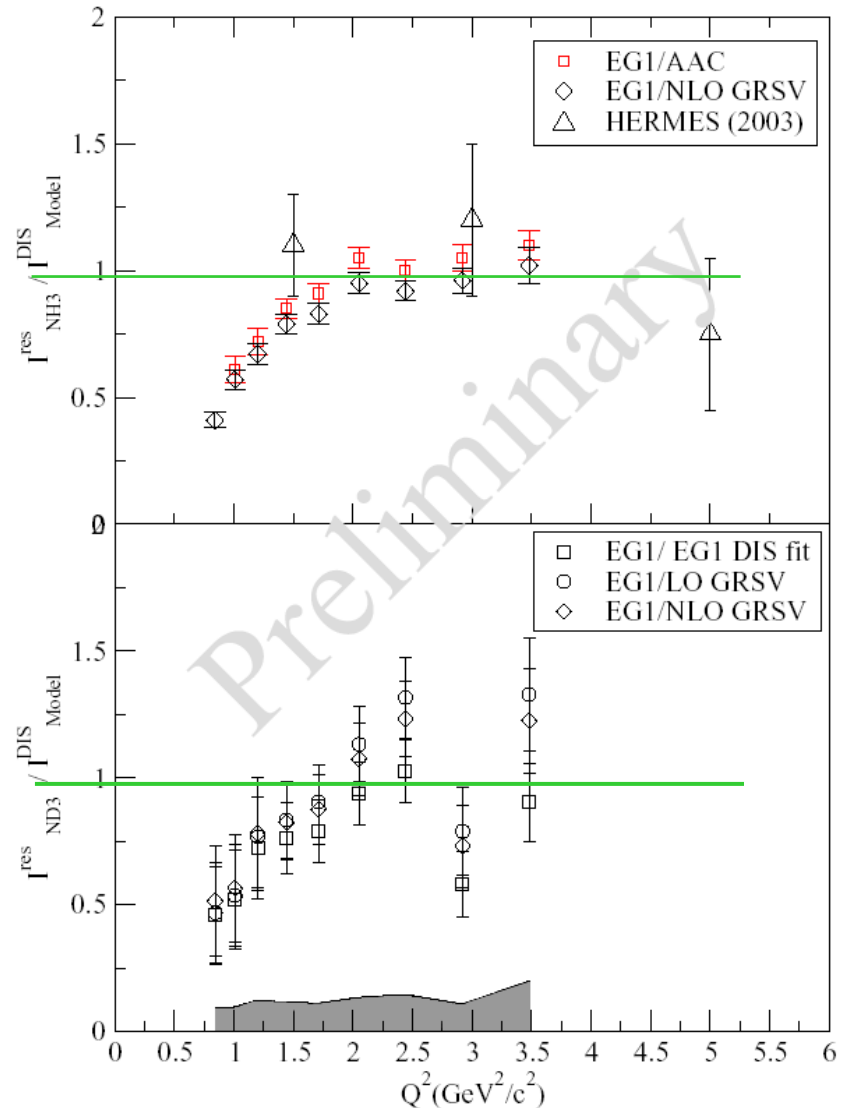
Duality (Cont.)

Duality can be tested in quantitative way constructing the ratio of

$$I^{RES} = \int_{x_{\min}}^{x_{\max}} g_1^{RES}(x, Q^2) dx$$

$$I^{DIS} = \int_{x_{\min}}^{x_{\max}} g_1^{DIS}(x, Q^2) dx$$

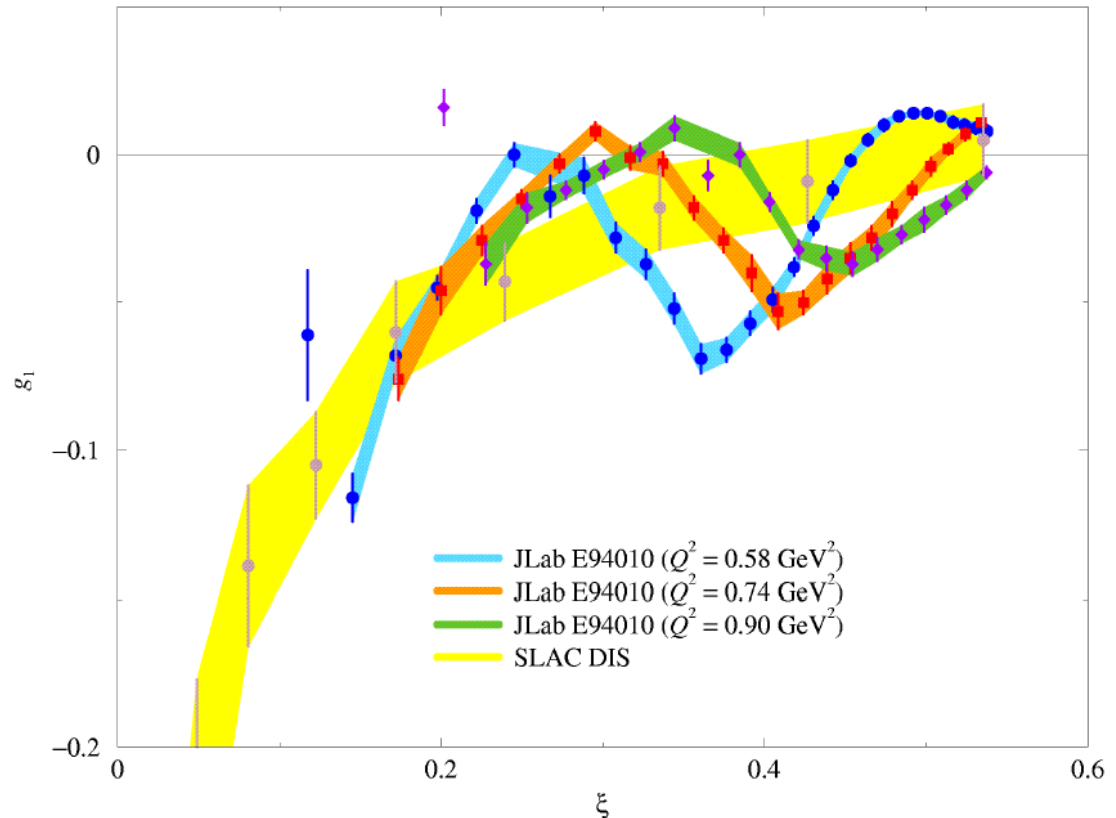
- ◆ Good agreements with previous HERMES results
- ◆ Ratio consistent with unity for $Q^2 > 2 \text{ GeV}^2$
- ◆ Significant deviation below



Duality (Cont.)

measured structure function seems follow quantitatively the Q^2 -evolved DIS measurements

- new experiment on ^3He target (E01-012) completed in 2003 is presently under analysis
- complementary measurement on proton and deuteron planned in Hall C (E03-109)



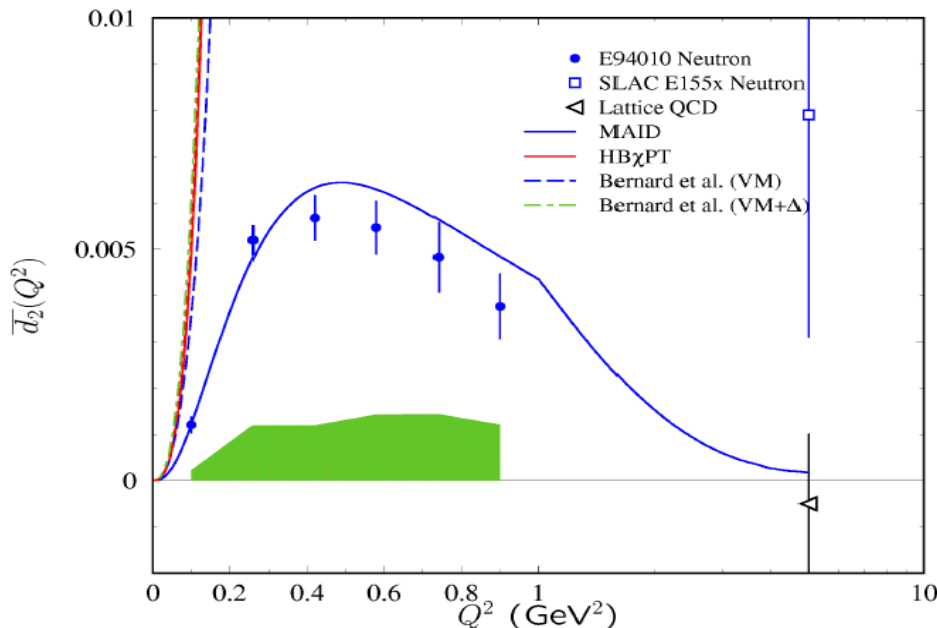
Higher Twists Effects in g_2

$$g_2(x, Q^2) = g_2^{WW}(x, Q^2) + g_2^{\text{H.T.}}(x, Q^2)$$

$$g_2^{WW}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 \frac{g_1(y, Q^2)}{y} dy$$



$$d_2(Q^2) = 3 \int_0^1 x^2 \left[g_2(x, Q^2) - g_2^{WW}(x, Q^2) \right] dx$$



- ◆ provide direct information on higher twist contributions in spin structure functions
- ◆ precise evaluation of d_2 using world data for g_1
- ◆ measured values are systematically greater than zero

Spin Observables in Exclusive Reactions

Asymmetries and Resonance Amplitudes

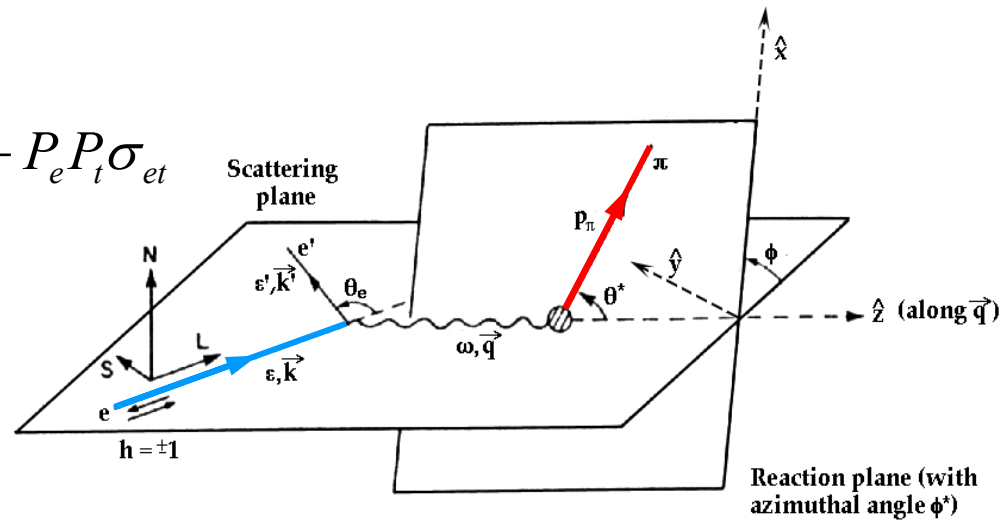
Electroproduction Cross Section

$$\sigma(W, Q^2, \theta^*, \phi^*) = \sigma_0 + P_e \sigma_e + P_t \sigma_t + P_e P_t \sigma_{et}$$

σ_0 : unpolarized cross section

$\sigma_e, \sigma_t, \sigma_{et}$: polarization cross sections

P_e, P_t : beam and target polarization



$$A_{et} = \frac{\sigma_{et}}{\sigma_0}$$

→ related to the inclusive asymmetries A_1 and A_2

$$A_e = \frac{\sigma_e}{\sigma_0}$$

contain complementary information to what accessible in inclusive measurements, powerful tool to investigate resonance structure

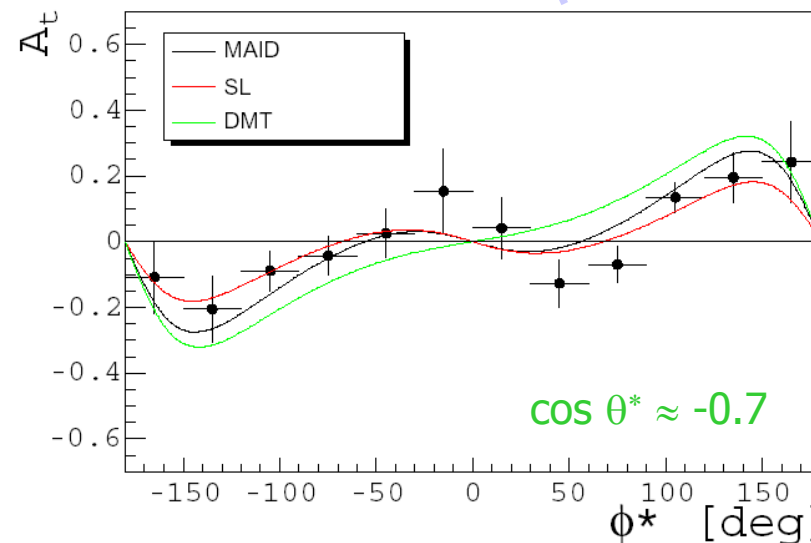
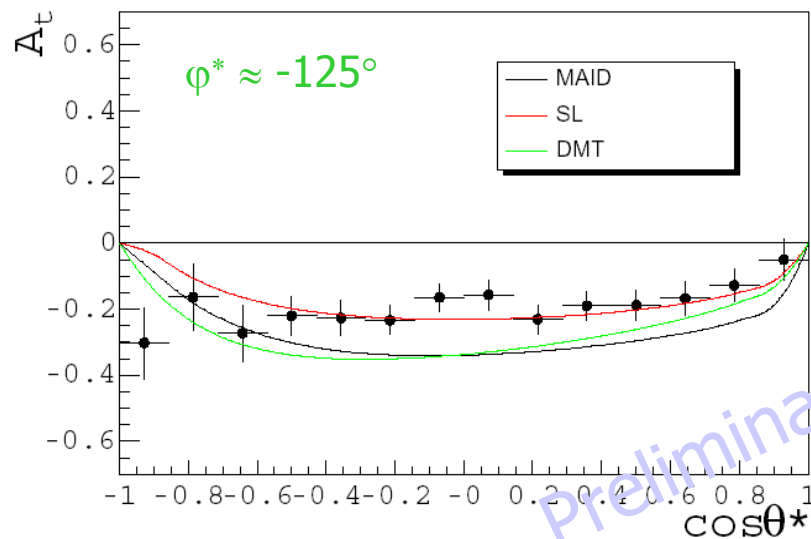
$$A_t = \frac{\sigma_t}{\sigma_0}$$

The $\Delta(1232)$ in π^0 production

$$Q^2 \approx 0.4 \text{ GeV}^2$$

$$1.2 < W < 1.25 \text{ GeV}$$

- ◆ At low Q^2 Δ production is dominated by the magnetic multiple M_1 (spin flip)
- ◆ At large Q^2 pQCD predicts $E_2/M_1 \rightarrow 1$
- ◆ Study of this transition requires extraction of small multipoles contribution \rightarrow model dependence
- ◆ Measured target asymmetry shows sensitivity to resonance and background contribution and provide constrain to model calculations

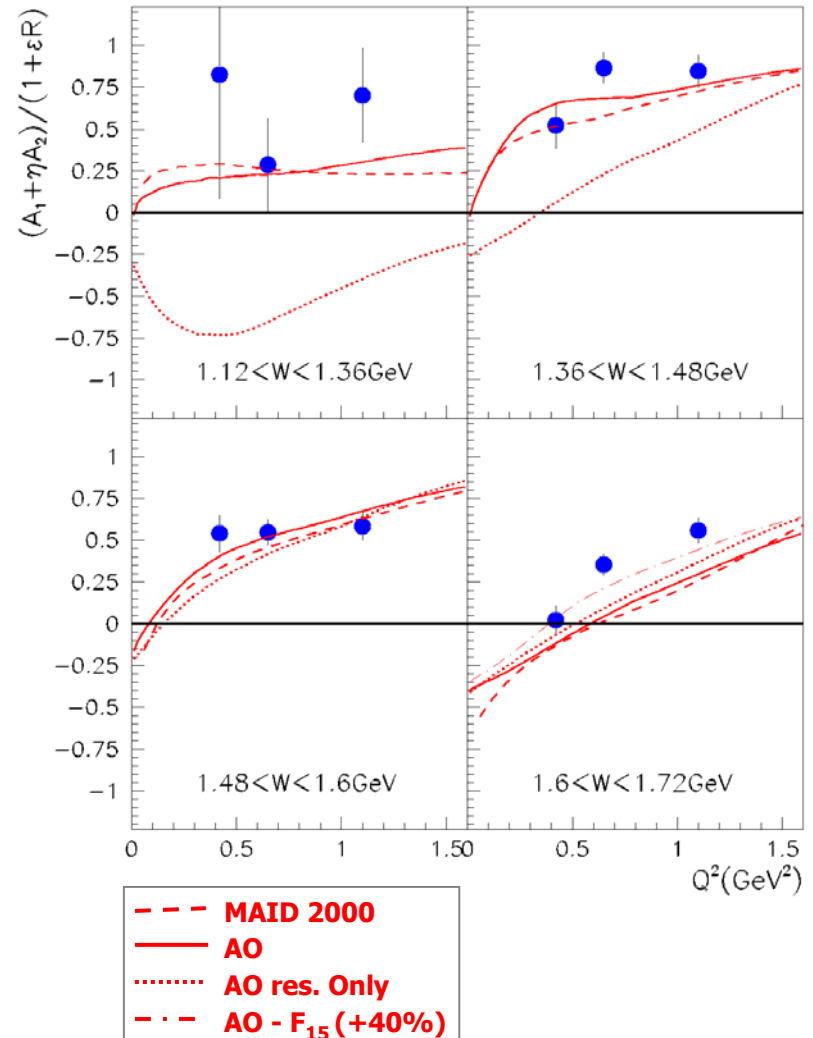


Resonance Contribution in $ep \rightarrow e'\pi^+ n$

$$E_0 = 2.5 \text{ GeV}$$

$$Q^2 \approx 0.5 \text{ GeV}^2$$

- ◆ First measurement of double spin asymmetry
- ◆ Strong coupling of π^+ channel with second and third resonance region states
- ◆ Dominance of resonance contribution for $W > 1.3 \text{ GeV}$
- ◆ Positive values of the measured asymmetry indicate dominance of $A_{1/2}$ amplitude
- ◆ Comparison with model predictions shows sensitivity single resonance contribution



η electroproduction

◆ η production channel is dominated by the decay of the $S_{11}(1535)$ resonance

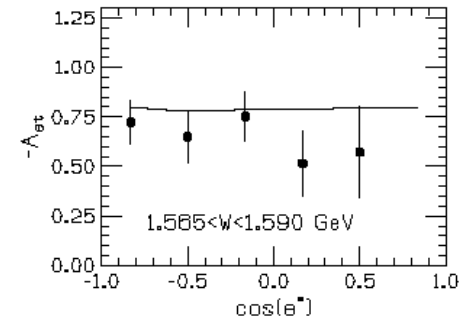
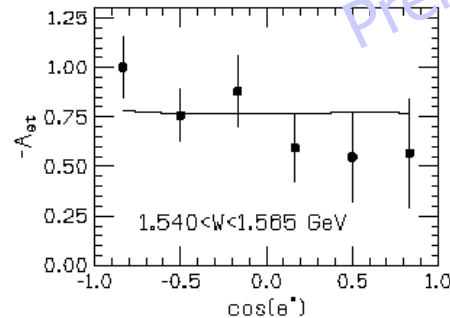
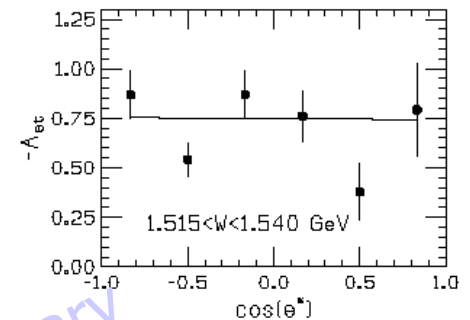
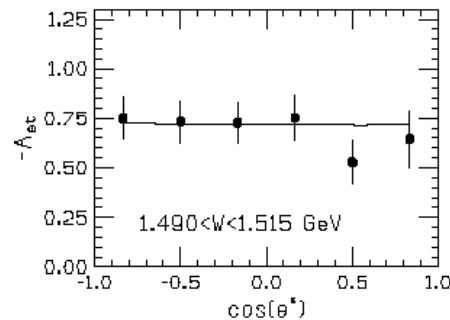
◆ in the the assumption of S_{11} dominance the double spin asymmetry is expected to be constant

$$A_{et} = D = \left(1 - \varepsilon \frac{E'}{E}\right)$$

◆ measured asymmetries are consistent with the hypothesis of S_{11} dominance

◆ good agreement with the prediction of eta-Maid model

$E_0 = 1.6$ GeV



→ see P. Bosted talk

Summary

- ◆ A broad physics program to study the nucleon spin structure in the non perturbative regime is in progress at Jefferson Lab
- ◆ These measurements aim at understanding the transition between hadronic and partonic degrees of freedom investigating phenomena such as resonance excitation, duality in spin structure functions, higher twists,...
 - ◆ Inclusive measurements have shown that spin structure functions undergo to a dramatic change as Q^2 varies between 0.1 and 2 GeV^2 .
 - ◆ Significant contribution from higher twist have been found in the same Q^2 range.
 - ◆ Measurement of spin polarizabilities indicates inconsistencies with χPT prediction.
 - ◆ Duality in spin structure functions is found to hold for $Q^2 > 2 \text{ GeV}^2$
 - ◆ Measurement of spin observables in exclusive channels shows strong sensitivity to resonance parameters and allow to put stringent constraints on effective models
- ◆ New measurements to extend and complete the existing program are planned in the near future